$\qquad$ Hour: $\qquad$ Date: $\qquad$

## How much will you make next year?

After much thought Mrs. Gallas has finally decided on permanent employee wages which are randomly assigned using the probability distribution $X$ given below. Additionally, at the end of every year she gives her employees an hourly raise. The bonuses are assigned randomly according to the probability distribution $Y$ given below. Assume $X$ and $Y$ are independent.

1. Find the mean, variance and standard deviation of the probability distribution of $X$, the hourly wages.

| $X$ | 9 | 12 | 15 |
| :--- | :--- | :--- | :--- |
| Probability | 0.30 | 0.45 | 0.25 |

Mean: $\qquad$ Variance: $\qquad$ Standard Deviation: $\qquad$
2. Find the mean, variance and standard deviation of the probability distribution of $Y$, the annual hourly raise.

| $Y$ | $\$ 1$ | $\$ 3$ |
| :--- | :--- | :--- |
| Probability | 0.70 | 0.30 |

Mean: $\qquad$ Variance: $\qquad$ Standard Deviation: $\qquad$
3. Let $N=$ the new hourly wage for the upcoming year $(X+Y)$.
a. What are all the possible new hourly wages for the new year?
b. What is the probability of an employee being assigned a $\$ 9$ wage AND a $\$ 1$ raise? Show your work.
c. Complete the table below for the probability distribution of $N=X+Y$ and find the mean and standard deviation.

| $N$ |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Probability |  |  |  |  |  |  |

Mean: $\qquad$ Variance: $\qquad$ Standard Deviation: $\qquad$
d. If $N=X+Y$, complete the following in terms of $X$ and $Y$ :

$$
\mu_{N}=\quad \sigma_{N}=
$$

Name: $\qquad$ Hour: $\qquad$ Date: $\qquad$

## Combining Probability Distributions

Important ideas:

## Check Your Understanding

Mrs. Chauvet recently had twins. Let $X=$ the number of diaper changes per day for Alyse and $Y=$ the number of diaper changes per day for Jocelyn. Based on a few weeks of careful records, the probability distributions of $X$ and $Y$ are as follows:

| Number of diapers <br> changed $x_{i}$ | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: |
| Probability $p_{i}$ | 0.05 | 0.25 | 0.60 | 0.10 |


| Number of diapers <br> changed $y_{i}$ | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: |
| Probability $p_{i}$ | 0.05 | 0.20 | 0.55 | 0.20 |
| Mean: $\mu_{Y}=4.9$ | SD: $\sigma_{Y}=0.768$ |  |  |  |

Define $T=X+Y$. Assume that $X$ and $Y$ are independent.
a. Find and interpret $\mu_{T}$.
b. Calculate and interpret $\sigma_{T}$.
c. Alyse wears Diaper size 1, which cost $\$ 0.238$ per diaper and Jocelyn wears Diaper size 2 which cost $\$ 0.2975$ per diaper. Find the mean and standard deviation of Mrs. Chauvet's total diaper cost per day.

